

Electromagnetically induced transparency with noisy lasers

Yanhong Xiao,^{1,2} Tun Wang,^{3,4} Maria Baryakhtar,⁵ Mackenzie Van Camp,⁶ Michael Crescimanno,⁷ Michael Hohensee,^{2,5} Liang Jiang,⁵ David F. Phillips,² Mikhail D. Lukin,⁵ Susanne F. Yelin,^{3,8} and Ronald L. Walsworth^{2,5}

¹*Department of Physics, Surface Physics Laboratory (National Key Laboratory), and Laboratory of Advanced Materials, Fudan University, Shanghai 200433, People's Republic of China*

²*Harvard-Smithsonian Center for Astrophysics, Cambridge, Massachusetts 02138, USA*

³*Department of Physics, University of Connecticut, Storrs, Connecticut 06269, USA*

⁴*Institute for Theoretical Physics, University of Innsbruck, 6020 Innsbruck, Austria*

⁵*Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA*

⁶*Department of Physics, Lawrence University, Appleton, Wisconsin 54912, USA*

⁷*Department of Physics and Astronomy, Youngstown State University, Youngstown, Ohio 44555-2001, USA*

⁸*ITAMP, Cambridge, Massachusetts 02138, USA*

(Received 22 August 2008; published 9 October 2009)

We demonstrate and characterize two coherent phenomena that can mitigate the effects of laser phase noise for electromagnetically induced transparency (EIT): a laser-power-broadening-resistant resonance in the transmitted intensity cross correlation between EIT optical fields, and a resonant suppression of the conversion of laser phase noise to intensity noise when one-photon noise dominates over two-photon-detuning noise. Our experimental observations are in good agreement with both an intuitive physical picture and numerical calculations. The results have wide-ranging applications to spectroscopy, atomic clocks, and magnetometers.

DOI: [10.1103/PhysRevA.80.041805](https://doi.org/10.1103/PhysRevA.80.041805)

PACS number(s): 42.50.Gy, 32.70.Jz, 42.50.Md

When a laser interacts with a resonant medium, phase noise in the laser's optical field can be converted to intensity noise [1]. For electromagnetically induced transparency (EIT) in atomic and other systems [2], such a deleterious noise conversion is of great interest because of the wide application of EIT in atomic clocks [3,4], magnetometers [5], quantum optics [6,7], and quantum communications [8–10]. Laser phase-noise-to-intensity-noise conversion in the absence of atomic ground-state coherence and its role in atomic-clock instability [1,11–13] and the effect of laser phase noise on photon-photon correlations in atomic vapor cells [6,7] have been studied previously. However, the role of EIT coherence in noise processes remains to be understood. In this Rapid Communication, we demonstrate and present intuitive models for two coherent noise phenomena that can mitigate the conversion of laser phase noise to intensity noise in EIT media: (i) a laser-power-broadening-resistant resonance observed in intensity cross correlations between the two EIT optical fields and (ii) resonant suppression of phase-noise-to-intensity-noise conversion, which occurs when one-photon noise (driven by laser phase noise) dominates two-photon-detuning noise. We find good agreement between our experimental and theoretical investigations of these two coherent phenomena, which should enable improved EIT measurements with realistic (noisy) lasers in a wide variety of systems.

In our experiments, we used warm ⁸⁷Rb vapor for studies of both Zeeman EIT with degenerate ground states and hyperfine EIT with ground electronic states split by ≈ 6.8 GHz. To observe EIT, we employed a vertical cavity surface emitting laser (VCSEL) operating on the ⁸⁷Rb D_1 line (795 nm) with a linewidth of 100 MHz, chosen for compatibility with real-world coherent-population-trapping (CPT) atomic clocks [12] and magnetometers. The large phase-noise bandwidth allows us to neglect other noise sources such as laser

intensity and polarization noises. For Zeeman EIT, we used the $5S_{1/2}, F=2$ -to- $5P_{1/2}, F'=1$ transition; for hyperfine EIT, we used the $5S_{1/2}, F=1, 2$ -to- $5P_{1/2}, F'=2$ transition. The VCSEL was stabilized to a dichroic atomic vapor laser lock [14]. We used vapor cells containing isotopically enriched ⁸⁷Rb heated to 40 °C, with a Ne buffer gas of either 2 or 40 Torr. The optical path through the vapor cell was less than one absorption length, suppressing propagation effects and simplifying comparisons between measurements and models. The vapor cell was housed in high-permeability magnetic shielding to screen external magnetic fields; a homogeneous magnetic field was applied as necessary by an internal solenoid. For Zeeman EIT, a linearly polarized monochromatic optical field was sent into the atomic medium. At the output, a quarter-wave plate and a polarizing beam splitter separated the circularly polarized components of the transmitted light. For each two-photon detuning, we recorded the ac transmission for ~ 200 μ s (longer times produced the same result) of the two polarizations and calculated $g^2(0)$ as defined below. For hyperfine EIT, we modulated the VCSEL at 3.42 GHz, half the ground-state hyperfine splitting, using a low-noise rf synthesizer; the ± 1 sidebands formed the two EIT fields coupling the two hyperfine ground states. The polarization of the input optical fields was circularized using a quarter-wave plate, and the total transmitted power through the atomic medium was detected.

First, we discuss the power-broadening-resistant resonance observed in intensity cross correlations of the two transmitted EIT optical fields, first observed in [6]. We find that the resonance line shape has a dual structure containing power-broadened and power-independent components as shown in Fig. 1. The narrow central peak in the cross-correlation spectrum lies within a broader structure and has a linewidth approximately equal to the intrinsic decay rate of the ground-state coherence, while the broader structure ex-

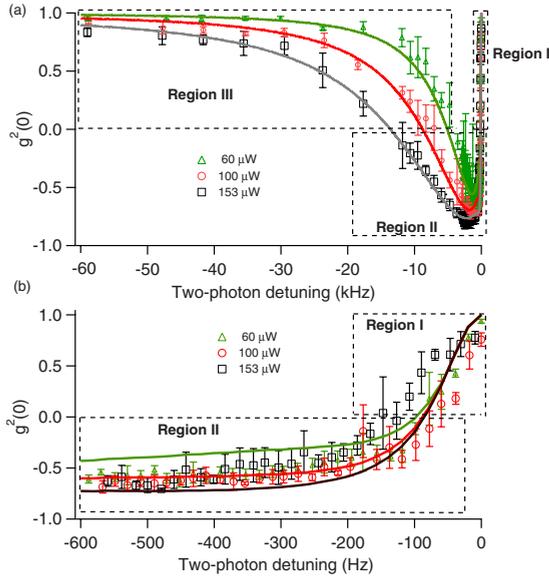


FIG. 1. (Color online) Cross correlation in the transmitted intensity fluctuations of Zeeman EIT vs two-photon detuning as measured (symbols) and calculated (lines). In (a) regions I–III of correlation, anticorrelation, and return to correlation described in the text are visible, while (b) shows the central region of (a) near zero two-photon detuning. The linewidth of the central peak is approximately the same for 60 and 100 μW data, and broader for 153 μW data, which was taken at higher magnetic gradient, showing that intrinsic decoherence determines the narrow resonance width. Only negative detuning is shown, as the experimental results are symmetric with two-photon detuning. 2 Torr Ne buffer gas and 3 mm laser beam diameter. In the calculation, an intrinsic decay rate of $\approx 2\pi \times 100$ Hz was used for all laser powers.

hibits a typical power broadening, as can be understood from an intuitive dark-state model below. Here, the cross correlation is defined by $g^{(2)}(0) \equiv \langle \delta I_1(t) \delta I_2(t) \rangle / \sqrt{\langle (\delta I_1)^2 \rangle \langle (\delta I_2)^2 \rangle}$, where $\delta I_{1,2}$ are the intensity fluctuations of the two EIT fields at the output of the vapor cell. Positive (negative) $g^{(2)}(0)$ indicates correlation (anticorrelation) between fluctuations in the two transmitted field intensities.

A simple theoretical model captures the relevant physics of these intensity cross-correlation measurements. For an optically thin Λ system with ground states $|a\rangle, |b\rangle$ and excited state $|e\rangle$, $g^{(2)}(0)$ is given by [6]

$$g^{(2)}(0) = \frac{\langle \text{Im}(\delta\rho_{ea})\text{Im}(\delta\rho_{eb}) \rangle}{\sqrt{\langle [\text{Im}(\delta\rho_{ea})]^2 \rangle \langle [\text{Im}(\delta\rho_{eb})]^2 \rangle}}. \quad (1)$$

Here $\langle \rangle$ represents an average over input field fluctuations and $\text{Im}(\delta\rho_{ea})$ and $\text{Im}(\delta\rho_{eb})$ are the imaginary components of fluctuations away from steady state of the atomic density-matrix elements corresponding to the optical coherences. In the dark-state basis, the numerator of Eq. (1), which determines the sign of $g^{(2)}(0)$, can be rewritten as

$$G^{(2)}(0) = \langle [\text{Im}(\delta\rho_{e+})]^2 \rangle - \langle [\text{Im}(\delta\rho_{e-})]^2 \rangle, \quad (2)$$

i.e., as the difference of the mean square of the optical coherence fluctuations involving the bright ($|+\rangle$) and the dark ($|-\rangle$) states defined as $|\pm\rangle = (\Omega_{1,2}|a\rangle \pm \Omega_{2,1}|b\rangle) / \Omega$, where

$\Omega_{1,2}$ are the complex Rabi frequencies for $|a, b\rangle \rightarrow |e\rangle$ transitions and Ω is the total two-photon Rabi frequency.

We modeled the dynamics in this simplified three-level Λ system using a Hamiltonian expressed in the dark state basis

$$H = \Omega|e\rangle\langle +| + \Delta|+\rangle\langle -| - \delta|e\rangle\langle e| + \text{H.c.}, \quad (3)$$

where δ and Δ are the one- and the two-photon detunings and H.c. represents the Hermitian conjugate. We included phenomenological damping terms for atomic excited-state and intrinsic ground-state relaxation, with relaxation rates γ and Γ , respectively. Three processes are present in this model: (i) the bright state is coupled to the excited state by the laser fields, incoherently optically pumping atoms into the dark state at a rate Ω^2/γ ; (ii) the dark $|-\rangle$ and bright $|+\rangle$ states are coherently coupled at a rate given by the two-photon detuning Δ ; and (iii) the dark and the bright states are incoherently coupled at rate Γ .

The sign of $G^{(2)}(0)$ can be evaluated from the optical coherences in Eq. (2). The zeros of $G^{(2)}(0)$ then provide an estimate of the width of the cross-correlation resonance (see Fig. 1). Because there is no direct coherent coupling between $|e\rangle$ and $|-\rangle$, the ρ_{e-} coherence can only be nonzero if coherence is established between the $|+\rangle$ and the $|-\rangle$ states. Such ground-state coherence (ρ_{+-}) is created from a population difference between the dark and the bright states at a rate proportional to the two-photon detuning Δ . When $|\Delta| \ll \Gamma \ll \Omega^2/\gamma$, atoms remain almost entirely in the dark state as decoherence suppresses ρ_{+-} and hence ρ_{e-} , and from Eq. (2) positive correlations between the intensity of the two transmitted EIT optical fields are observed (see region I of Fig. 1). When $\Gamma < |\Delta| \ll \Omega^2/\gamma$, dark-state population dominates over bright-state population and it drives the ρ_{+-} coherence faster than it decoheres. This allows ρ_{e-} to dominate ρ_{e+} , leading to anticorrelations in the transmitted field intensities (region II of Fig. 1). The crossover between regions I and II sets the width of the narrow central peak and occurs for $\Delta \approx \Gamma$, which is independent of laser power. For $|\Delta| > \Omega^2/\gamma \gg \Gamma$, the atomic population oscillates between the bright and the dark states faster than optical pumping repopulates the dark state, which reduces the rate at which ρ_{+-} is produced, and hence returns the system to a positive $G^{(2)}(0)$ (region III).

Figure 1 shows an example of cross-correlation [$g^{(2)}(0)$] data for Zeeman EIT. Regions I–III described above are clearly seen, with the transition from region I to II determining the width of the power-broadening-resistant resonance. A low buffer gas pressure Rb vapor cell (2 Torr Ne) was used in the measurements shown in Fig. 1 to reduce pressure broadening and hence effects from the second excited state [15]. The measured half width at half maximum of the central peak of the cross-correlation resonance is ≈ 100 Hz for all laser power [Fig. 1(b)], which is consistent with the extrapolated zero-power EIT linewidth for this system, and is limited by residual magnetic field inhomogeneity as shown by the slight broadening of the 153 μW data under larger field gradient than the other two laser powers, whereas the conventional power-broadened EIT linewidth is much greater. These measurements demonstrate that the central

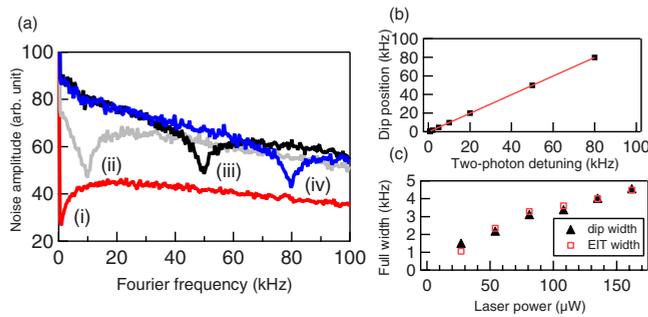


FIG. 2. (Color online) (a) Measured noise spectra of total transmitted power for hyperfine EIT. Two-photon detunings of (i) 1, (ii) 10, (iii) 50, and (iv) 80 kHz. (b) Dip center frequencies vs two-photon detuning (symbols); line represents $dip\ center = detuning$. (c) Widths of dips and EIT resonances are equal at all input laser powers. (Two-photon detuning = 50 kHz.) Laser power $\approx 170\ \mu\text{W}$ for plots (a) and (b). 0.85 mm beam size and 2 Torr Ne buffer gas for (a)–(c).

cross-correlation peak is immune to power broadening. Note that, for lower laser power—insufficient to optically pump atoms into the dark state—complete anticorrelation between the transmitted field intensities is not reached, which is consistent with the picture presented above. An analytical model using the above analysis and phenomenologically including the coherent return of atoms [16] to the laser beam reproduces the observed cross-correlation results (lines in Fig. 1) and will be presented elsewhere.

Potential applications of the power-broadening-resistant $g^{(2)}(0)$ resonance include the measure of the intrinsic coherence rate even with high laser power and atomic clocks and magnetometers for which there is often a trade-off between a narrow resonance and a sufficient signal-to-noise-ratio (SNR) because of power broadening. While the data reported above rely upon Zeeman EIT, the analysis is for a general three-level system and therefore is applicable to hyperfine EIT and atomic clocks. Using the data shown in Fig. 1, and generalizing to orthogonal linear polarization hyperfine EIT [17], we estimate the stability to be $3 \times 10^{-11} \tau^{-1/2}$, which is comparable to the current CPT clock performance [3]. This stability can be further improved for the cross-correlation resonance with an increased laser power, which allows for higher SNR without broadening the resonance, potentially enabling a superior atomic reference.

Next, we discuss the second topic of this Rapid Communication: the resonant suppression of laser phase-noise-to-intensity-noise conversion in EIT media, governed by the relative importance of one-photon and two-photon-detuning noises. Figure 2(a) shows examples of measured intensity noise spectra for hyperfine EIT at several two-photon detunings (2 Torr Ne buffer gas, 170 μW laser power). In each case, the intensity noise drops at a Fourier frequency equal to the two-photon detuning [Fig. 2(b)], with a linewidth equal to the EIT linewidth [Fig. 2(c)] and a line shape determined by diffusion of atomic coherence in and out of the laser beam [16]. Numerical analysis indicates that the reduced intensity noise near two-photon resonance results from phase correlations between the two EIT optical fields [18]. When the fields' two-photon detuning Δ is nonzero but much smaller

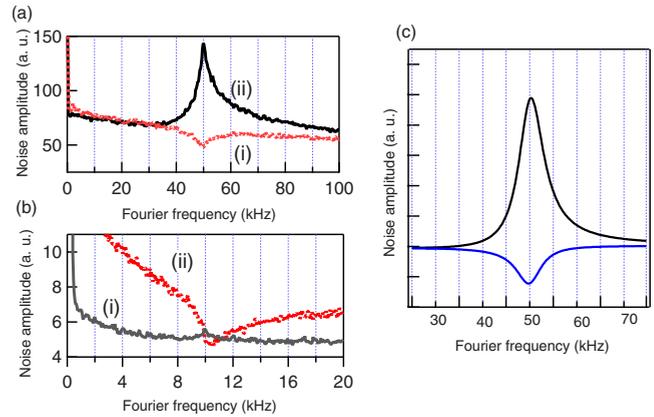


FIG. 3. (Color online) (a) and (b) Measured transition between resonant (i) suppression and (ii) enhancement of laser phase-noise-to-intensity-noise conversion in hyperfine EIT. (See text for experimental details.) (c) Examples of calculated noise spectra for no two-photon phase noise (dip) and extra phase noise (peak) at $\Delta = 50$ kHz.

than the excited-state linewidth or the laser linewidth, Fourier components of phase fluctuations in one optical field that are offset by Δ from that field's central frequency will form EIT with the other optical field; this EIT will suppress absorption and conversion of laser phase noise to intensity noise within the EIT linewidth.

This observed resonant *drop* in laser phase-noise-to-intensity-noise conversion for an EIT system is in striking contrast to the *enhanced* intensity noise observed before [4,19]. The qualitatively different behaviors in the two cases can be understood by noting that the effect of laser phase noise in a two-level system is analogous to two-photon-detuning noise in EIT. We find experimentally that either a resonant peak or a dip can appear in EIT intensity noise spectra, determined by the relative importance of one-photon noise (arising from laser phase noise) and two-photon-detuning noise (due to phase noise in the rf signal used to modulate the laser for hyperfine EIT or to magnetic field noise for Zeeman EIT [20]). In particular, when an EIT system is subjected to sufficient two-photon-detuning noise, the EIT phase correlations arising from laser phase noise are destroyed, and the resonant dip in the intensity noise spectrum is transformed into a noise peak.

We performed two experiments to illustrate the importance for EIT noise spectra of the relative magnitude of one-photon noise and two-photon-detuning noise. First, we measured hyperfine EIT noise spectra in a 2 Torr Ne buffer gas cell, which had significant one-photon noise induced by the VCSEL's phase noise, but small two-photon-detuning noise (-95 dBc/Hz at 10 kHz offset from the 3.42 GHz signal modulating the VCSEL). With this setup, we found a dip in the EIT intensity noise spectrum [Fig. 3(a), curve (i)]. With sufficient added phase noise to bring the two-photon-detuning noise to dominance (-75 dBc/Hz at 10 kHz offset), conventional EIT for the transmitted fields was unaffected, but the noise dip was transformed into a peak [Fig. 3(a), curve (ii)]. Next, we employed a high-pressure buffer gas cell (40 Torr Ne), which broadened the one-photon reso-

nance linewidth and hence reduced the conversion of laser phase noise to one-photon intensity noise [21], such that the two-photon-detuning noise dominated without adding extra noise to the rf modulation signal. With this setup, we observed a noise peak for hyperfine EIT on one-photon resonance [Fig. 3(b), curve (i)]. A noise dip re-emerged by detuning the laser from one-photon resonance by less than half a linewidth, which increased the conversion of laser phase noise to one-photon intensity noise, so that it dominated the effect of two-photon-detuning noise [Fig. 3(b), curve (ii)]. Our numerical modeling agrees with the observed EIT noise spectra described above [Fig. 3(c)]: noise spectra peaks and dips are found at a Fourier frequency equal to the two-photon detuning; dips always appear in the absence of two-photon detuning noise, while peaks appear when sufficient two-photon detuning noise is added. Model line shapes are Lorentzian instead of exhibiting the sharper structure of experimental data due to lack of coherence return in the simple model. A small offset of the observed peak and dip location may be attributed to the slope underlying the intensity noise background determined by phase-noise spectra of the laser and the synthesizer and their frequency-dependent conversion into laser intensity noise, which necessitates further investigation.

These results show that transmitted intensity noise spectra can be used as a broadband measure of EIT resonance location without scanning the two-photon detuning. The location and the linewidth of the noise dip or peak indicate the EIT resonance frequency and the linewidth directly. In addition, the noise peak or dip is detectable for two-photon detunings

much greater than the narrow EIT linewidth. Combining these noise spectra techniques with a broadband laser source could provide extremely broadband coverage [22]. Off-resonant detection of the two-photon EIT resonance via noise spectra could also be used in sensing or imaging applications where other resonant effects (e.g., absorption) are of concern. Additionally, we note the possibility that input laser phase noise could serve as a seed field to amplify quantum fluctuations in an EIT medium and thereby enable improved noise spectroscopy [23]. Finally, this technique has a broad applicability due to the simple nature of its coupling of laser noise to the evolution of ground-state coherence. As such this technique should be applicable to many coherent media including EIT in rare-earth-doped crystals and color centers in diamond.

In conclusion, we demonstrated and characterized two coherent phenomena associated with EIT and laser phase noise: a laser-power-broadening-resistant resonance in the transmitted intensity cross correlation of EIT optical fields, and a resonant suppression or enhancement of laser phase-noise-to-intensity-noise conversion, governed by the relative magnitude of one-photon noise and two-photon-detuning noise. The present results may enable improved EIT measurements with realistic (noisy) lasers, and hence be useful for applications such as atomic clocks, magnetometers, quantum optics, and imaging.

We are grateful to I. Novikova, J. Kitching, and J. Vanier for useful discussions. This work was supported by ONR, the Smithsonian Institution, and NSF.

-
- [1] J. C. Camparo and J. G. Coffey, *Phys. Rev. A* **59**, 728 (1999).
 - [2] M. Fleischhauer *et al.*, *Rev. Mod. Phys.* **77**, 633 (2005).
 - [3] J. Vanier, *Appl. Phys. B: Lasers Opt.* **81**, 421 (2005).
 - [4] A. Godone, S. Micalizio, and F. Levi, *Phys. Rev. A* **66**, 063807 (2002).
 - [5] M. Martinelli *et al.*, *Phys. Rev. A* **69**, 043809 (2004).
 - [6] V. A. Sautenkov, Y. V. Rostovtsev, and M. O. Scully, *Phys. Rev. A* **72**, 065801 (2005); G. Ariunbold *et al.*, e-print arXiv:quant-ph/0603025.
 - [7] L. S. Cruz *et al.*, *Eur. Phys. J. D* **41**, 531 (2007); C. L. Garrido Alzar *et al.*, *Europhys. Lett.* **61**, 485 (2003).
 - [8] M. D. Lukin, *Rev. Mod. Phys.* **75**, 457 (2003).
 - [9] A. Sinatra, *Phys. Rev. Lett.* **97**, 253601 (2006).
 - [10] M. T. L. Hsu *et al.*, *Phys. Rev. Lett.* **97**, 183601 (2006).
 - [11] T. Yabuzaki, T. Mitsui, and U. Tanaka, *Phys. Rev. Lett.* **67**, 2453 (1991).
 - [12] J. Kitching *et al.*, *J. Opt. Soc. Am. B* **18**, 1676 (2001).
 - [13] J. Kitching *et al.*, *Opt. Lett.* **26**, 1507 (2001).
 - [14] K. L. Corwin *et al.*, *Appl. Opt.* **37**, 3295 (1998).
 - [15] I. Novikova *et al.*, *J. Opt. Soc. Am. B* **22**, 44 (2005).
 - [16] Y. Xiao *et al.*, *Phys. Rev. Lett.* **96**, 043601 (2006).
 - [17] T. Zanon *et al.*, *Phys. Rev. Lett.* **94**, 193002 (2005).
 - [18] S. E. Harris, *Phys. Rev. Lett.* **70**, 552 (1993); M. Fleischhauer and T. Richter, *Phys. Rev. A* **51**, 2430 (1995); A. F. Huss, R. Lammegger, C. Neureiter, E. A. Korsunsky, and L. Windholz, *Phys. Rev. Lett.* **93**, 223601 (2004); E. E. Mikhailov, V. A. Sautenkov, Y. V. Rostovtsev, A. Zhang, M. S. Zubairy, M. O. Scully, and G. R. Welch, *Phys. Rev. A* **74**, 013807 (2006); D. Yu and J. Chen, *Phys. Rev. Lett.* **98**, 050801 (2007).
 - [19] J. C. Camparo, J. G. Coffey, and R. P. Frueholz, *Phys. Rev. A* **58**, 3873 (1998).
 - [20] The phase noise between two independent lasers exciting EIT creates both one- and two-photon detuning noises.
 - [21] J. G. Coffey, M. Anderson, and J. C. Camparo, *Phys. Rev. A* **65**, 033807 (2002).
 - [22] X. Xu *et al.*, *Nat. Phys.* **4**, 125 (2008).
 - [23] S. A. Crooker *et al.*, *Nature (London)* **431**, 49 (2004); N. Muller and A. Jerschow, *Proc. Natl. Acad. Sci. U.S.A.* **103**, 6790 (2006).